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Energetics and mechanics of human running on surfaces of different stiffnesses

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1Harvard Division of Health Sciences and Technology, and 5Artificial Intelligence Laboratory, Massachusetts Institute of Technology, Cambridge 02138; 3Concord Field Station, Museum of Comparative Zoology, Harvard University, Bedford 01730; 2Division of Engineering and Applied Sciences, Harvard University, Cambridge 02138; 4United States Army Research Institute for Environmental Medicine, Natick 01760; and 6Department of Physical Medicine and Rehabilitation, Harvard Medical School, Spaulding Rehabilitation Hospital, Boston, Massachusetts 02114

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Kerdok, Amy E., Andrew A. Biewener, Thomas A. McMahon, Peter G. Weyand, and Hugh M. Herr. Energetics and mechanics of human running on surfaces of different stiffnesses. J Appl Physiol 92: 469–478, 2002; 10.1152/ japplphysiol.01164.2000.—Mammals use the elastic components in their legs (principally tendons, ligaments, and muscles) to run economically, while maintaining consistent support mechanics across various surfaces. To examine how leg stiffness and metabolic cost are affected by changes in substrate stiffness, we built experimental platforms with adjustable stiffness to fit on a force-plate-fitted treadmill. Eight male subjects [mean body mass: 74.4 ± 7.1 (SD) kg; leg length: 0.96 ± 0.05 m] ran at 3.7 m/s over five different surface stiffnesses (75.4, 97.5, 216.8, 454.2, and 945.7 kN/m). Metabolic, ground-reaction force, and kinematic data were collected. The 12.5-fold decrease in surface stiffness resulted in a 12% decrease in the runner’s metabolic rate and a 29% increase in their leg stiffness. The runner’s support mechanics remained essentially unchanged. These results indicate that surface stiffness affects running economy without affecting running support mechanics. We postulate that an increased energy rebound from the compliant surfaces studied contributes to the enhanced running economy.

IN THEIR GROUNDBREAKING work, McMahon and Greene (29) investigated the effects of surface stiffness (k_{surf}) on running mechanics. Their study sought to determine whether it was possible to build a track surface that would enhance performance and decrease injury. Their work showed that a range of k_{surf} values existed over which a runner’s performance was enhanced by decreasing foot-ground contact time (t_{c}), decreasing the initial spike in peak vertical ground reaction force (f_{peak}), and increasing stride length. Tracks built within this enhanced performance range at Harvard University, Yale University, and Madison Square Garden have been shown to increase running speeds by 2–3% and to decrease running injuries by 50% (29). Despite the success of these “tuned tracks,” the mechanisms underlying the performance enhancement are not clearly understood.

A major assumption of McMahon and Greene’s (29) was that the running leg and surface could be represented as a simple spring and mass (Fig. 1). McMahon and Cheng (27) subsequently described the leg spring as having two stiffnesses: k_{leg} and k_{vert}. The k_{leg} is the actual leg stiffness describing the mechanical behavior of the leg’s musculoskeletal system during the support phase and is calculated from the ratio of f_{peak} to the compression of the leg spring (\Delta l, defined in Eq. B4)

$$k_{leg} = \frac{f_{peak}}{\Delta l}$$

(1)

In distinction, k_{vert} is the effective vertical stiffness of the runner. This stiffness serves as the mechanism by which the direction of the downward velocity of the body is reversed during limb contact (27, 30). Therefore, k_{vert} describes the vertical motions of the center of mass during the ground contact phase (27, 30). The k_{vert} can be calculated from the ratio of f_{peak} to the maximum vertical displacement of the center of mass during contact (\Delta y_{total}), measured from the onset of limb contact (heel-strike) to midstep

$$k_{vert} = \frac{f_{peak}}{\Delta y_{total}}$$

(2)

Farley et al. (12) and He et al. (19) determined that, for a given ground stiffness, k_{leg} changes little with speed. Later experiments showed that k_{leg} changes when animals run on surfaces of different stiffnesses (16, 18). It was specifically shown that human hoppers’ k_{leg} adjustments were mainly due to changes in both ankle joint stiffness and leg posture (14). However, Arampatzis et al. (3) provided evidence that the knee joint is...
RUNNING ON SURFACES OF DIFFERENT STIFFNESSES

Fig. 1. Spring-mass model representing a runner’s leg in contact with a compliant surface. \(l_c\), Uncompressed leg length; \(m_r\), mass of the runner represented as a point mass located at the hip; \(\Delta l\), maximum vertical displacement of the center of mass; \(\theta\), angle of the leg spring at first ground contact; \(k_{leg}\), spring constant of the runner’s leg; \(m_{track}\), effective mass of the running surface; \(d_{surf}\), amount the running surface deflects; \(k_{surf}\), spring constant of the running surface; and \(f_{grf}\), vertical ground reaction force.

The goal of this study is to relate human running biomechanics to energetics on surfaces of different stiffnesses. We expect that differences in the metabolic cost of running on various surfaces are likely related to \(k_{leg}\), variations observed by Farley et al. and Ferris et al. (13, 17, 18). Specifically, we expect a less flexed knee to account for a reduction in metabolic cost (30), as well as an increase in \(k_{leg}\) (3, 18).

In this study, we investigate the energetics and mechanisms of running on surfaces having a stiffness range from 75 to 945 kN/m. This range of stiffnesses was selected to incorporate the range of McMahon and Greene’s “tuned track” (29) and to extend the work of similar recent studies (16–18). We hypothesize that the metabolic cost of forward human running reaches a minimum when the \(k_{leg}\) of the runner is maximized on surfaces of decreased stiffness. We expect a cost reduction to result from a change in leg posture, whereby the knee is less flexed or straighter during stance (30). Running with a straighter leg should improve the limb’s mechanical advantage, thereby reducing the amount of muscle force and muscle volume recruited to support body weight (5). We also anticipate that a reduction in metabolic cost could result from an increased energy return to the runner from the more compliant surfaces (14). Last, we expect that the runner’s support mechanics will remain virtually unaffected across the above-defined range of \(k_{surf}\).

EXPERIMENTAL METHODS

General procedures. Eight healthy male subjects (body mass: 74.4 ± 7.1 (SD) kg; leg length: 0.96 ± 0.05 m) ran at 3.7 m/s on a level treadmill, fitted with track platforms of five different stiffnesses (see descriptions below). All subjects wore the same flat-soled running shoes. Approval was granted from Harvard University’s Committee on the Use of Human Subjects in Research, and subjects provided signed, informed consent before participation. Subjects ran for 5 min on each track platform stiffness in a mirrored fashion (running on stiffest to least stiff and then least stiff to stiffest). Beaded strings hung from the ceiling to give the runner a tactile sign as to where he needed to run so that his midstep corresponded with the fore-aft center of the track platform. Video was also used to ensure that the runner was both centered and lateral enough not to be stepping on both sides of the track simultaneously. If a runner was unable to avoid the seam between tracks, he was asked to move laterally and run on one track or the other. We recorded ground reaction force (1,000 Hz) using a force plate (model OR6–5–1, Advanced Medical Technology, Newton, MA) mounted within the treadmill (22). Kinematic data were collected at 60 Hz using an infrared motion analysis system (MacReflex by Qualysis), and oxygen uptake was measured using a closed gas-collection Douglas bag setup. Oxygen and carbon dioxide contents of the collected gas samples were analyzed using Ametek (Pittsburgh, PA) S-3A O2 and CD-3A CO2 analyzers equipped with an Ametek CO2 sensor (P-61B) and flow controller (R-2). The analyzers were calibrated before each run with gas by pumping several balloons of known gas mixture (16.23% O2 and 4.00% CO2 medical gas mixture; AGA Gas, Billerica, MA) through them. Force-plate and kinematic data were obtained simultaneously, and oxygen consumption (V\(_{O2}\)) data were sampled during the fourth and fifth minutes of running to ensure that the subject was at a steady state. Subjects participated in two separate trials so that they ran on each platform stiffness four times. Averages were taken on each day and then averaged together for all variables measured.

Experimental platform design. We built platforms with an adjustable stiffness for our running surface. Because the experiments were conducted on a treadmill, the running surface was limited to platforms that would fit within the size limitations of the treadmill. We used a treadmill fitted with an AMTI force plate (22) that was accessible to the Douglas bag oxygen analysis setup.

We tested five \(k_{surf}\) based on ranges found in the literature (14, 16, 18, 29). The McMahon and Greene (29) tuned track stiffness range is between 50 and 100 kN/m. Because of size limitations of the existing treadmill and earlier work done by Farley and Morgenroth (15) and Ferris et al. (17), we designed our variable stiffness track platforms to span from...
75.4 kN/m to stiffnesses of 97.5, 216.8, 454.2, and 945.7 kN/m. The indoor track at Harvard University has a \( k_{surf} \) of \(-190 \) kN/m, allowing for a 9-mm deflection for a 75-kg runner (assuming a runner exerts roughly 2.3 times body weight at midstance). For a similar runner, our track would result in 22.4-, 17.4-, 7.8-, 3.7-, and 1.8-mm deflections \( d_{surf} \), respectively, according to the following equation

\[
d_{surf} = \frac{2.3 \cdot m_s \cdot g}{k_{surf}}
\]

where \( m_s \) is the mass of the runner, \( g \) is the gravitational constant, and \( k_{surf} \) is the stiffness of the track. The factor 2.3 is an estimate of how much the \( f_{peak} \) exceeds body weight during a running step.

The platform design is shown in Fig. 2. Garrolite (G-10, Current, East Haven, CT) was chosen as the material for the track platforms because it met all of the design criteria described below and in Appendix A and could be easily machined. The design consisted of two G-10 planks \((1.22 \times 0.254 \times 0.014 \) m\) rigidly supported in the front and simply supported in the rear by 0.016-m-thick acrylic. By moving the treadmill rollers in at either end of the belt surface, enough slack was provided to fit the platforms under the belt directly on top of the force plate. Rollers were added to the existing treadmill to reroute the treadmill belt over the platforms, and a frame was built (not shown) to hold the platform in place on top of the force plate during testing. The rear support was movable so that, by simply adjusting it in closer to or farther away from the front support, the stiffness of the running surface was increased or decreased, respectively.

Once installed, the stiffness of each platform was calibrated by applying static loads to a person and measuring force \( f_{peak} \) from the force plate and deflection \( d_{surf} \) from an LVDT cable extender \( \pm 0.25\% \), Celeesco Transducer Products (Eq. 3).

As described in Appendix A, the inertial effects of the running platform motion compared with the forces exerted by the runner’s leg can be considered negligible if the effective mass of the platform is \(<17\% \) of \( m_s \), \((11.43 \) kg for the smallest runner studied). The effective masses \((6.88, 8.88, 4.94, 2.65, \) and \( 5.39 \) kg\) gave inertial forces of \(-41.43, -30.41, -10.04, -3.33, \) and \(-0.42 \) N, respectively. These forces were \(<2.5\% \) of the peak forces exerted by the runner and so were ignored.

Given that the running surface was a compliant surface having the potential to return energy to the runner, we also calculated the energy return of our variable-stiffness track platform. We did this by using the track deflection to derive the potential energy at each track stiffness \( E_{track} \)

\[
E_{track} = \frac{1}{2} k_{surf} d_{surf}^2
\]

Multiplying this energy by two times the stride frequency results in the mechanical power delivered from the track to the runner. This was then related to a measurement of the metabolic power \( E_{metabol} \) consumed by the runner at each track stiffness.

**Force-plate measurements.** A runner’s support mechanics, defined as \( f_{peak} \), \( t_e \), duty factor, stride frequency, step length, one-half of the angle swept by a runner’s leg during ground contact \( \theta \), and the total vertical displacement of the center of mass, can be calculated from the force-plate data and the assumption that the leg can be represented by an undamped, linear spring \((22)\). These parameters can then be indirectly used to calculate the mass-spring characteristics of the runner’s leg. Custom LabVIEW (version 4.0.1) software was used to acquire the force-plate data. The force plate was calibrated by applying known loads to the plate before and after each set of running trials and sampling its output using the same software. The derivation of all of the above parameters is described in Appendix B.

**Kinematic measurements.** To obtain information on the posture of the limb in contact with the ground, we used an infrared camera system (Mac Reflex; Qualysis) to follow markers that were specifically placed on the subjects. Markers were positioned on the skin overlying the greater trochanter, the lateral epicondyle of the femur, and the lateral malleolus, so that the angle that the lower leg made with the upper leg (knee angle) could be determined.

Kinematic data were collected simultaneously and synchronized with the force-plate data (using an infrared light-emitting diode in the camera’s field of view that gave a voltage pulse that was recorded when the light-emitting diode was switched on). Kinematic data were analyzed using the Maxdos software from Mac Reflex (Qualysis) and incorporated into a Matlab (version 4.0) program to calculate the knee angle at midstep. The program also calculated the series minimum height points of the greater trochanter marker for several strides over the 10-s collection period. This marker was used to estimate the position of a runner’s center of mass, and its minimum trajectory was used to define the midpoint of each step when force application reached its peak \((13, 19, 26)\).
Measuring metabolic cost. To quantify the metabolic cost of human running, we used the indirect calorimetry method, as described previously. After the runners ran for 3 min, we collected the expired air for 2 min using two Douglas bags (1 per minute), a mouthpiece, and a nose clip, which were attached to the runner via a special headpiece equipped with a one-way valve. The rate of VO2 (ml/min) was then calculated using the volume of the expired air (from a dry-gas volume meter; Parkinson-Cowan), room and vapor pressure corrections, and the percentage of CO2 and O2 values. We converted the rate of VO2 into energy consumption using an energy equivalent of 20.1 J/ml O2 (6) and divided by 60 s/min to obtain $E_{\text{metab}}$ in watts.

Kram and Taylor (23) define the rate of metabolic consumption ($E_{\text{metab}}$) in terms of a cost coefficient, $C_0$

$$E_{\text{metab}} = C_0 \left( \frac{1}{t_0} \right) (F_{\text{bw}})$$

where $C_0$ is an empirical measure of the metabolic cost of applying ground force to support the body’s weight ($F_{\text{bw}}$) (4, 31). For this investigation, the $C_0$ is computed to determine the effect of $k_{\text{surf}}$ on the energetics of supporting the runner’s body weight.

Statistical methods. A 1 x 5 ANOVA with a Scheffe post hoc test of condition means was used to assess the effect of $k_{\text{surf}}$ on the parameters of interest: $t_c$, peak vertical force, stride time, stride frequency, step length, $\theta$, $\Delta y_{\text{total}}$, displacement of the limb with respect to the track displacement, $E_{\text{metab}}$, $C_0$, $k_{\text{leg}}$, $k_{\text{vert}}$, $\Delta l$, overall system stiffness, and knee angle. $P$ values $<0.05$ were considered significant for all tests.

RESULTS

The runner’s support mechanics were nearly invariant across the 12.5-fold change in $k_{\text{surf}}$ of the experimental treadmill platform (Fig. 3), whereas their metabolic rate dropped dramatically with $k_{\text{surf}}$ (Fig. 6).

The results of the Scheffe post hoc test revealed that, in virtually every case, the support mechanics remained essentially unchanged over the four stiffest surfaces tested. The basis for a significant difference in the ANOVA results reported below was found to be due to the data recorded for the lowest stiffness track surface.

As shown in Fig. 3, the effect of $k_{\text{surf}}$ on $t_c$ ($P = 0.0001$, $F = 8.7$), duty factor ($P = 0.0001$, $F = 18.45$), step length ($P = 0.0001$, $F = 8.51$), stride frequency ($P = 0.0001$, $F = 15.35$), $\theta$ ($P = 0.0001$, $F = 8.44$), and $f_{\text{peak}}$ ($P = 0.009$, $F = 4.19$) were significant. However, the data across these support mechanics showed only a small difference between the two stiffness extremes. The source of the difference occurred at the lowest stiffness, with the remaining four stiffnesses being essentially the same.
In particular, when the support mechanics means are compared, there was a 4% decrease in \( t_c \), step length, and \( \theta \) between the stiffest and least stiff surfaces studied. A 7% decrease in duty factor, 3% decrease in stride frequency, and a 5% increase in \( f_{\text{peak}} \) were also observed between these stiffness extremes.

The post hoc test revealed that the runners also maintained a nearly constant total leg plus track platform stiffness \( (k_{\text{tot}}) \) over the observed range of conditions \( (P = 0.0207, F = 3.45) \) (Fig. 4C). To achieve this, the runner’s \( k_{\text{leg}} \) increased by 29% with decreasing \( k_{\text{surf}} \) \( (P = 0.0001, F = 23.76) \) (Fig. 4A). Given that the runner’s \( f_{\text{peak}} \) did not change greatly over the substrate stiffness range (Fig. 3F), the observed increase in the runner’s \( k_{\text{leg}} \) most likely resulted from a decrease in the amount that his leg spring was compressed \( (\text{length} / \text{height} = 92.58) \) over the four stiffest surfaces further supports \( k_{\text{leg}}\). Given that the runners’ knee angle at midstep to running over all surfaces (Fig. 7). Knee angle increased 2.5% as \( k_{\text{surf}} \) decreased \( (P = 0.0001, F = 16.35) \). Thus only a slight straightening of the leg was observed.

Last, to test our hypothesis that the track itself may return significant energy to the runner, we calculated the track platform’s mechanical power \( (E_{\text{track}} \text{Eq. 4}) \) at each \( k_{\text{surf}} \) and compared this with the reduction in \( E_{\text{metab}} \) of the runner (Eq. 5) (Fig. 8). The results show that, for every watt of mechanical power returned from the track platform, there exists the possibility of a 1.8-W \( E_{\text{metab}} \) savings to the runner \( (R^2 = 0.99) \).

**DISCUSSION**

Our results support the hypothesis that the metabolic cost of running at an intermediate speed is progressively reduced and that the spring stiffness of the leg is progressively increased as \( k_{\text{surf}} \) is decreased from 945.7 to 75.4 kN/m. However, in contrast to our hypothesis that a change in limb posture is the principal factor underlying a change in both \( k_{\text{leg}} \) and metabolic cost, we found that only small changes in knee angle were associated with the observed 29% increase in \( k_{\text{leg}} \) and 12% decrease in \( E_{\text{metab}} \). Our data do not provide

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**Fig. 4.** When subjects ran at a constant speed (3.7 m/s) over 5 different surface stiffnesses (74–945 kN/m), there was a 29% change in their leg stiffness \( \gamma = 1.37 \ln(x) + 22.4, R^2 = 0.87 \) (A) and a 16% decrease in leg compression \( \gamma = 0.008 \ln(x) + 0.091, R^2 = 0.86 \) with decreasing surface stiffness (D). The overall stiffness of the system \( \gamma = 0.175 \ln(x) + 14.46, R^2 = 0.4 \) (C) and the effective vertical stiffness of the runner \( \gamma = 0.81 \ln(x) + 29.31, R^2 = 0.66 \) (B) remained essentially unchanged.
any additional insight into the mechanism for $k_{\text{leg}}$ adjustment but do suggest that a reduction in metabolic cost occurs as the elastic rebound provided by a more compliant surface replaces that otherwise provided by a runner’s leg.

Previous work indicated that runners adjust the stiffness of their limbs to maintain virtually constant support mechanics on surfaces of different stiffnesses (3, 14, 16, 18, 28). Although these studies provide insight into the mechanics of human running, they did not specifically examine the metabolic cost of running on compliant surfaces. One study (30) looked at deep-knee-flexed running and its effect on $k_{\text{vert}}$ and $V_{O_2}$ but did not incorporate $k_{\text{leg}}$ or compliant surfaces. Our goal was to expand on these earlier studies and examine how changes in limb-substrate stiffness interactions affect the metabolic cost of running. Consequently, we

\[ y = -1.25 \ln(x) + 137.29, R^2 = 0.97 \]

Fig. 7. The angle formed between the runner’s upper and lower legs was defined from markers placed at the greater trochanter, lateral epicondyle of the femur, and lateral malleolus. This knee angle increased 2.5% as surface stiffness decreased \[ y = -1.25 \ln(x) + 137.29, R^2 = 0.97 \], giving rise to a slightly straighter leg on the softer surfaces studied. Values are means ± SD.

\[ E_{\text{metab}} = C_0 \times (1/t_c) \times F_{\text{bw}}, \] where $E_{\text{metab}}$ is the rate of metabolic consumption, $C_0$ is an empirical measure of the metabolic cost of applying ground force to support the body’s weight ($F_{\text{bw}}$), and $t_c$ is the period of foot-ground contact. Values are means ± SD.
ever, we found a reduction in metabolic rate with over a constant (high) stiffness substrate (5). As a previous studies of animals moving at steady speeds and gaits. This assumption is supported by analysis assumes that animals maintain a uniform ground stiffness without affecting the center of mass in the latter portion of the contact phase is provided by the elastic recoil of the running surface rather than the biological springs in the runner's leg, the metabolic cost of running is reduced. We believe that these reductions in the metabolic cost of operating leg springs are probably explained by decreases in the mechanical work and shortening velocity performed by the muscles active during foot-ground contact.

Although we had hypothesized that reductions in metabolic cost and increases in $k_{leg}$ would be achieved predominantly via changes in knee angle, it seems evident that this mechanism cannot fully account for these changes. The change in $k_{leg}$ is likely due to a combination of local joint stiffness variation and overall limb posture adjustment (15). Whereas our study provided some indication that the leg becomes straighter at midstep on less stiff surfaces (Fig. 7), the change at the knee was small and would require a large sensitivity to have an effect on externally developed knee torque. Therefore, this small change in knee angle could only account for a minority of the reductions in metabolic cost and increases in $k_{leg}$ that we observed on more compliant surfaces.

Our hypothesis also anticipated that the decrease in $E_{metab}$ might well be explained by an enhanced energy return from the more compliant track platforms. The elastic surface could actually be assisting the runner by assuming some of the cost necessary to operate the leg spring, reducing the amount of mechanical work required, and thereby allowing the leg muscles to operate more isometrically. Reductions in relative shortening velocities would reduce metabolic cost in two ways. First, the increased force per unit area of active muscle would reduce the volume of muscle required to support the body's weight. Second, the $E_{metab}$ consumed per unit of active muscle is also reduced when the muscles shorten through a lesser distance (20).

To lend support for these ideas, experiments were conducted to characterize the track-runner interaction. The dynamic calibration of the four most compliant experimental track platforms showed a linear relationship between force and displacement ($R^2 = 0.96, 0.97, 0.95, \text{and } 0.94$ from least to most stiff) with little hysteresis (damping ratio <0.1). Hence, the track can indeed be considered an elastic substrate capable of storing and returning mechanical energy. Also, by calculating the resonant period of the track-plus-runner system at the least stiff surface (~0.2 s) and comparing the result to the contact times of the runners at this same stiffness (0.21 ± 0.02 s), we conclude that the track has sufficient time to return its stored energy to the runner. Last, our results show a consistent linear

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Fig. 8. Change in the runner's metabolic power ($E_{metab}$) as a function of the change in mechanical power delivered from the track platforms ($E_{track}$) from the stiffest surface ($K_s$). The power delivered from the compliant track is derived from the mechanical energy due to the track spring (Eq. 4) multiplied by the runner's stride frequency. For every watt delivered from the track platforms, there exists a potential 1.8-W reduction in metabolic power ($\gamma = 1.80x$, $R^2 = 0.99$). Values are means ± SD. $K_n$, surface stiffness where $n = 1, 2, 3, 4$.

---

The close relationship between the reductions in metabolic rates and the increased mechanical power returned by the track to the runner in the latter portion of foot-ground contact (Fig. 8) offers a straightforward explanation. This close relationship strongly suggests that, when a greater share of the elastic rebound elevating the center of mass in the latter portion of the contact phase is provided by the elastic recoil of the running surface rather than the biological springs in the runner's leg, the metabolic cost of running is reduced. We believe that these reductions in the metabolic cost of operating leg springs are probably explained by decreases in the mechanical work and shortening velocity performed by the muscles active during foot-ground contact.
relationship between the reduction in $\dot{E}_{\text{metab}}$ and track mechanical power output across all surfaces studied (Fig. 8). These results suggest that the track has the capacity to save the runner 1.8 W of $\dot{E}_{\text{metab}}$ for every watt of mechanical power that it returns.

Although our results support the fact that running on a decreased $k_{\text{surf}}$ results in a reduction of metabolic cost and an increase in $k_{\text{leg}}$ without affecting support mechanics, future studies need to be done to find a true metabolic minimum. Our measurements were designed to examine surfaces that were within a stiffness range that had already demonstrated an enhanced running performance (29). However, support mechanics are progressively altered to accommodate extreme decreases in $k_{\text{surf}}$. As mentioned above, our results support our hypothesis that these support mechanics would remain fairly constant over the 12.5-fold change in $k_{\text{surf}}$ but also show a significant change in these variables at the lowest $k_{\text{surf}}$ studied. This raises the possibility of a trend in data as $k_{\text{surf}}$ goes even lower. McMahon and Greene’s (29) work supports this speculation. We also anticipate that, as $k_{\text{surf}}$ decreases even further and the virtual consistency of the support mechanics seen at the higher stiffnesses is lost, there would exist a true metabolic minimum. Studies that looked at running on surfaces with extremely low stiffness, such as a trampoline and pillows (30) or sand (24), which also have high damping ratios, indicate that runners likely increase the amount of center-of-mass work that they perform and thus substantially increase their cost of locomotion (24). We propose that a study be done to examine lower $k_{\text{surf}}$ values than were studied here to determine at what substrate stiffness a true metabolic minimum exists as a relation of speed. We believe that there exists an optimal ratio of $t_s$ to surface resonant period that can be used for the future design of tracks and even running shoes to minimize the cost of running.

Summary. Our study sought to link the mechanics and energetics of human running on surfaces of different stiffnesses. The results show that both metabolic cost and $k_{\text{leg}}$ change when $k_{\text{surf}}$ is manipulated. The metabolic reduction is largely due to the track’s elastic energy return assisting the runner’s leg spring. Although the mechanism for $k_{\text{leg}}$ adjustment still remains unclear, our results support the hypothesis that human runners adjust $k_{\text{leg}}$ to maintain consistent support mechanics across different surfaces.

This study has served to link previous studies on animal locomotion and to open the door to future investigations on locomotory mechanics and energetics. Understanding how metabolism, speed, and $k_{\text{leg}}$ relate to substrate mechanics will not only lead to advances in running shoe technology and track design, but may also motivate the development of highly adaptive orthotic and prosthetic leg devices that change stiffness in response to speed and ground surface variations, enabling the physically challenged to move with greater ease and comfort.

APPENDIX A

Experimental Track Platform Design

The design of the variable-stiffness track platform was based on simply supported, two-point bending beam theory. Pilot studies showed that this configuration would work well within the size limitations of the treadmill (0.102-m maximum height from the force plate to beneath the belt, 1.22-m long × 0.457-m wide force plate, and 0.5 × 2.64-m overall belt surface). Materials and dimensions were chosen based on the maximum deflection ($y_{\text{max}}$) of the center of the beam according to the factor of safety (FS) associated with the loads that would be applied in running ($F$) or

\[
y_{\text{max}} = -\frac{FL^3}{48EI}
\]

\[
FS = \frac{\sigma_u}{\sigma_{\text{max}}}
\]

where $L$ is the length of the beam, $E$ is Young’s modulus, $I$ is the area moment of inertia, $\sigma_u$ is the ultimate stress of the material, and $\sigma_{\text{max}}$ is the maximum allowable stress of the material.

Another design criterion was that the track platform mass needed to be small enough so that the inertial forces due to the movement of the platform would be negligible compared with the forces exerted by the runner’s leg. By modeling the leg and platform surface as a two-mass and two-spring system with a damper, we found that the effective mass of the platform had to be <12 kg (or 17% of the $m_t$) in order for the platform’s inertia to represent <10% of the peak force developed by a 72-kg runner. Therefore, given that the masses of the actual runners were from 67.3 to 81.5 kg, the effective mass of the track platforms ($m_{\text{track}}$) had to be <11.4–13.9 kg to meet this criterion.

The inertial effects of the track platforms on measurements obtained from the force plate could be obtained by calculating the effective mass of the platforms. The $m_{\text{track}}$ was estimated by treating the track as a harmonic oscillator and finding the damped frequency ($\omega_d$). $\omega_d$ was measured by striking the platform and plotting the displacement vs. time for the free vibration of the track surface (14). This was accomplished by mounting the LVDT cable extender at the center edge of the platform for each stiffness configuration, with the platform resting in position on top of the AMTI force plate and under the treadmill belt. The $\omega_d$ was computed from the period of vibration ($T_d$) or

\[
\omega_d = \frac{2\pi}{T_d}
\]

The equation describing the envelope of the free vibration curve can be used together with the damped natural frequency of the track to obtain the natural frequency and the damping ratio of the track surfaces

\[
x = \pm A e^{-\omega_d t}
\]

\[
\omega_d = \omega_n \sqrt{1 - \xi^2}
\]

where $x$ defines the envelope of free vibration, $A$ is the amplitude of free vibration, $\omega_n$ is the natural frequency, and $t$ is time. With the use of Eqs. A4 and A5, the natural frequency of the platform was calculated to be 105 rad/s, thus resulting in a negligible damping ratio of $\xi \approx 0.07$. Hence the $m_{\text{track}}$ was estimated from the $k_{\text{surf}}$ and the $\omega_d$, or
The $m_{\text{track}}$ was then used, together with the second derivative of the displacement curves (to obtain acceleration), to estimate the inertial force ($F_{\text{inertial}}$) of the track platforms using

$$F_{\text{inertial}} = m_{\text{track}} \frac{d^2x}{dt^2}$$  \hfill (A7)

**APPENDIX B**

**Derivation of the Force-Plate Parameters**

LabVIEW (version 4.0.1) was used to acquire the force-plate data and output the parameters of the runner's support mechanics ($t_{\text{peak}}, t_c, \text{stride time}, \text{stride frequency}, \text{step length}, \theta$, and the vertical displacement of the center of mass). Because of the vibrational noise from the treadmill belt, motor, and track (22), we filtered the force data using a low-pass, third-order Butterworth double-reverse filter. The smoothed curve for the ground reaction force was used for analysis. The $t_{\text{peak}}$ is the force at midstep and was taken to be the maximum value of this curve. The duration of the force provided a measure of the $t_c$ as well as total stride (right foot to right foot time) ($t_c + t_a = \text{dur}_{\text{tot}}$, where $t_a$ is the period the foot is in the air and $\text{dur}_{\text{tot}}$ is total duration) that were then used to calculate the stride frequency (freq) and step length (SL) (distance traveled by the center of mass during one $t_c$)

$$\text{freq} = \frac{\text{Hz}}{\text{dur}_{\text{tot}}}$$  \hfill (B1)

$$\text{SL} = t_c \bar{u}_x$$  \hfill (B2)

where $u_x$ is the horizontal (forward) velocity. With the additional input of the runner's leg length ($l_o$) measured from the runner's greater trochanter to the floor while standing straight legged, we calculated $\theta$ (see Fig. 1) from

$$\theta = \sin^{-1}\left(\frac{\text{SL}}{2l_o}\right)$$  \hfill (B3)

Because the ground reaction force is equal to the runner's $m_f$ times his acceleration, we were able to calculate the $\Delta Y_{\text{total}}$ of the runner by twice integrating the vertical acceleration of the center of mass over time ($t_c$).

To account for the displacement of the variable-stiffness surfaces ($d_{\text{surf}}$) in relation to the runner's $\Delta Y_{\text{total}}$, we calculated $d_{\text{surf}}$ from the calibrated values obtained for $k_{\text{surf}}$ and the forces obtained from the force plate (Eq. 3, where $2.3 \times m_c = t_{\text{peak}}$ from force plate).

The above variables were then used to calculate the mass-spring characteristics of the runner's leg. The maximum $\Delta Y$ was calculated by using the runner's $t_c, \theta$, and the actual $\Delta Y_{\text{limb}}$ (18, 26)

$$\Delta Y = \Delta Y_{\text{limb}} + l_o(1 - \cos \theta)$$  \hfill (B4)

$$\Delta Y_{\text{limb}} = \Delta Y_{\text{total}} - d_{\text{surf}}$$  \hfill (B5)

Because the $t_{\text{peak}}$ occurs at the same time that the center of mass is at its lowest height, the stiffness of the leg spring ($k_{\log}$) was calculated using the ratio of $t_{\text{peak}}$ to maximum leg compression (13, 19, 26) (Eq. 1). Similarly, the effective vertical spring stiffness was calculated using the peak force and the total displacement of the center of mass of the system (Eq. 2).

The total displacement is used in calculating $k_{\text{vert}}$ rather than the actual displacement of the runner alone, because, on less stiff surfaces, $k_{\text{vert}}$ is affected by the displacement of the surface (18). If the actual (or relative) displacement is used, the possibility exists that vertical stiffness could assume a negative value (the runner moves in the opposite direction at midstep in an effort to maintain a constant displacement of the system's center of mass), which is nonsensical.

Overall stiffness of the system ($k_{\text{totL}}$) was calculated as the sum of the $k_{\log}$ and the track platform stiffness ($k_{\text{surf}}$) in series

$$\frac{1}{k_{\text{totL}}} = \frac{1}{k_{\log}} + \frac{1}{k_{\text{surf}}}$$  \hfill (B6)

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